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| Title        | Updating and mathematical performance: Implications for children in lower primary  |
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Kerry Lee & Rebecca Bull

UPDATING AND MATHEMATICAL  
PERFORMANCE: IMPLICATIONS  
FOR CHILDREN IN LOWER  
PRIMARY

# Math Performance in Singapore

- ◎ Singapore has performed well in international comparisons of mathematics achievement
  - Trends in International Mathematics and Science Study
  - Programme for International Student Assessment
- ◎ A relatively large tail-end compared to other high performing systems
- ◎ Around 5.5% of children struggle with math on entry to primary schools

# Contributing Variables

## ⦿ System

- Societal expectation
- Education system
- Effort and quality of teachers

## ⦿ Individual

- Social or motivational (e.g., Ashcraft, Kirk, & Hopko, 1998)
- Biological (see Geary, 1993, for a review)
- Cognitive

# Working Memory

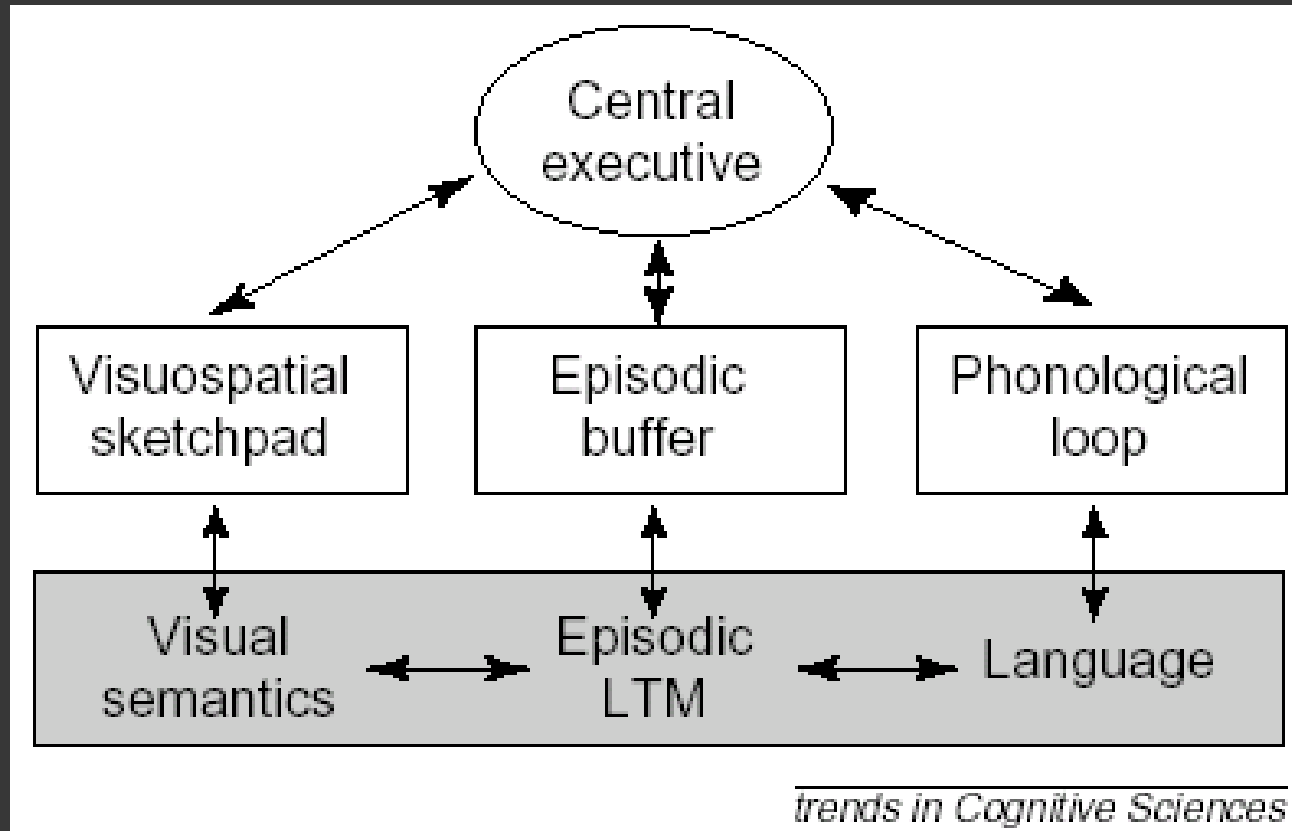
# What is Working Memory?



⦿  $259 + 36 = ?$

⦿  $764 / 4 = ?$

# Baddeley (2000)

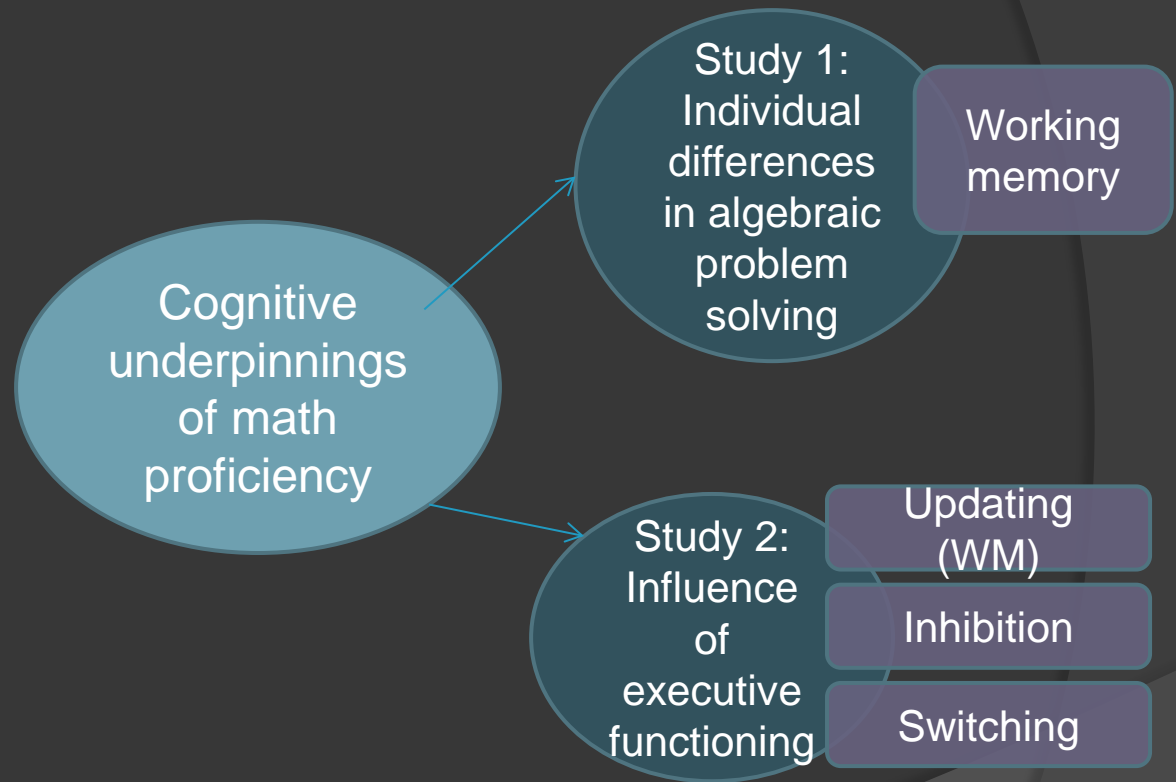


# Working Memory and Mathematical Performance

- Central executive measures predicted early mathematical performance
  - Bull, Johnston, and Roy (1999), Bull and Scerif (2001)
- Standardised working memory scores predicted children's academic standing in mathematics with 83% accuracy
  - Gathercole and Pickering (2000)

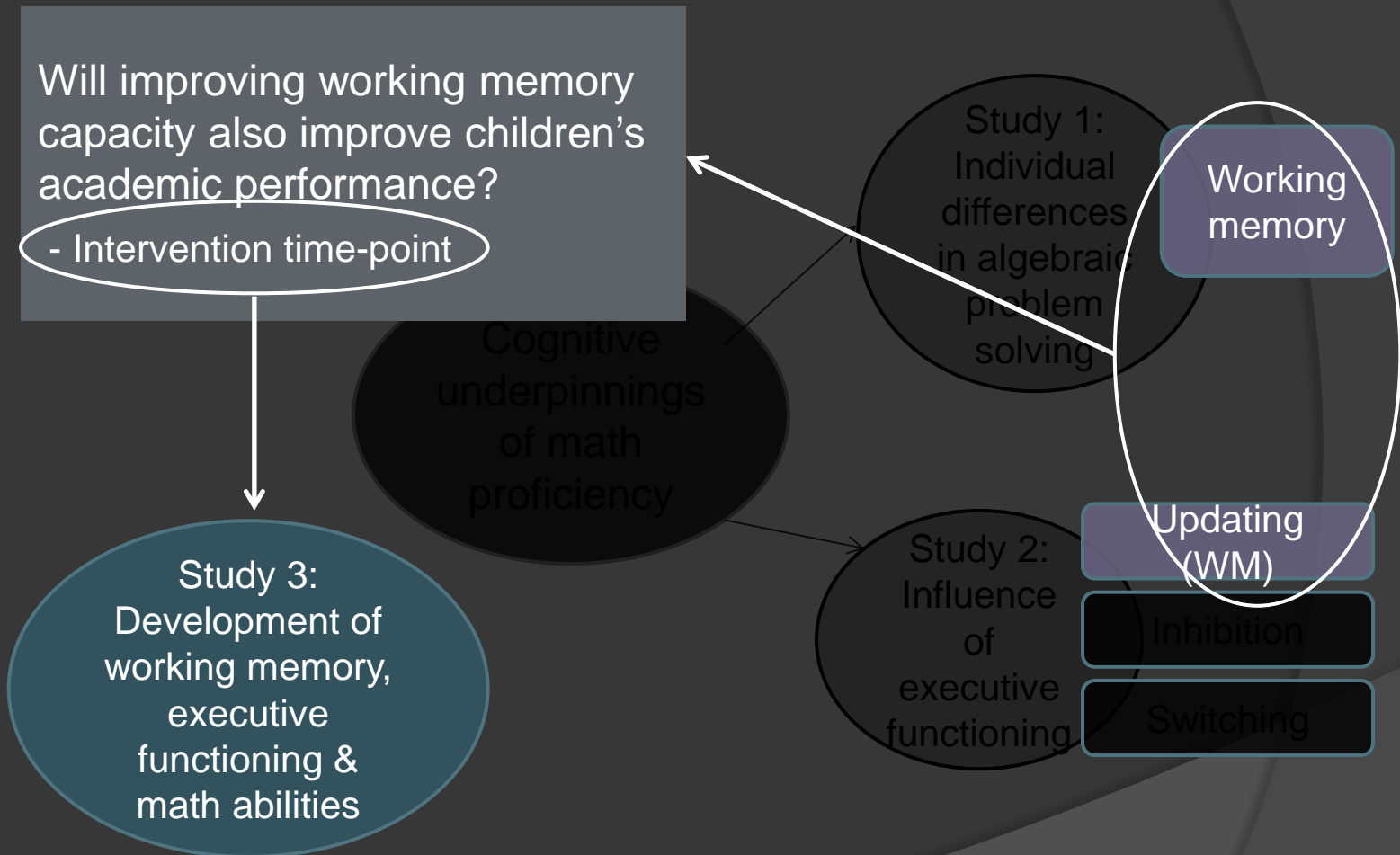


# Cognitive Underpinnings



Lee et al. (2004) *Jn Exp Child Psych*  
Lee et al. (2009) *Jn Edu Psych*

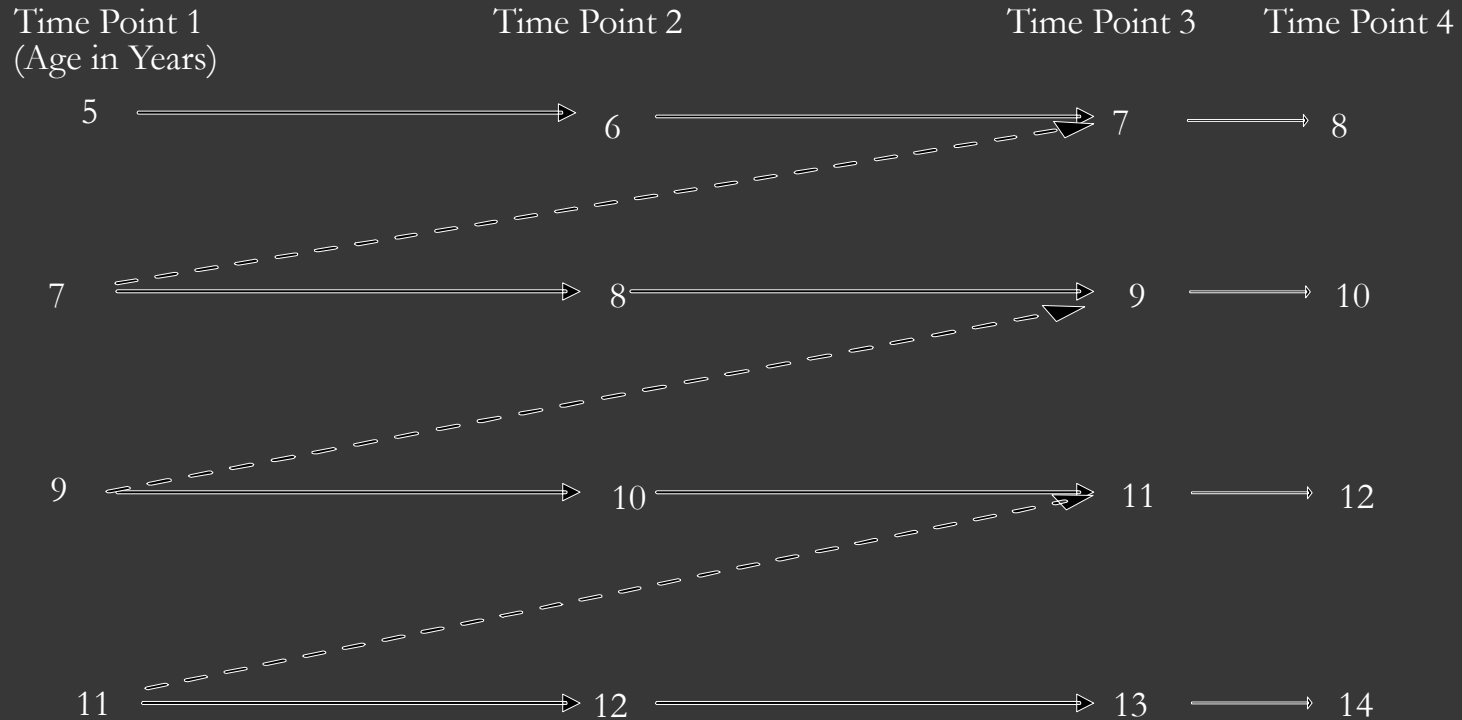
# Cognitive Underpinnings



# The Present Study

- ◉ Examined the relation between working memory/updating (WMU) and mathematical performance
  - Does the relation between WMU and mathematical performance remained the same from Kindergarten to Sec 3?
  - To what extent do earlier capacities in WMU and mathematics contribute to their later development?
  - Does performance in kindergarten affect the rates of growth in WMU and mathematics?

# Cohort-Sequential Design



~ 673 children  
spread over 4 cohorts,  
81 school at Wave 4

# Instruments

## ◉ Executive functioning

- Inhibitory efficiency
  - Flanker
  - Simon
  - Antisaccade Mickey
- Switching efficiency
  - Switch conditions from Flanker and Simon
  - Picture–symbol

- Updating capacity
  - Animal Updating
  - Mr. X
  - Listening Recall

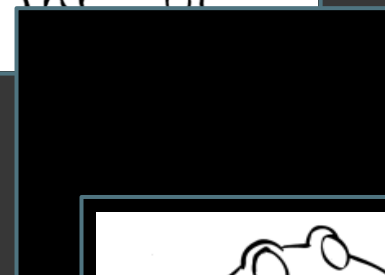
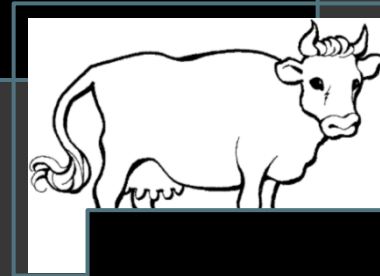
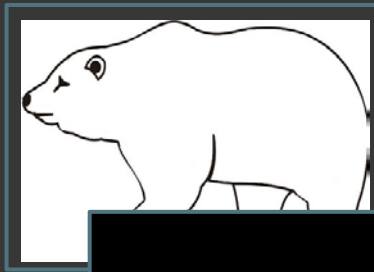
## ◉ Standardised mathematical tasks

- Wechsler Individual Achievement Test
  - Number Operations
  - Mathematical Reasoning

## ◉ Curricular based mathematical tasks

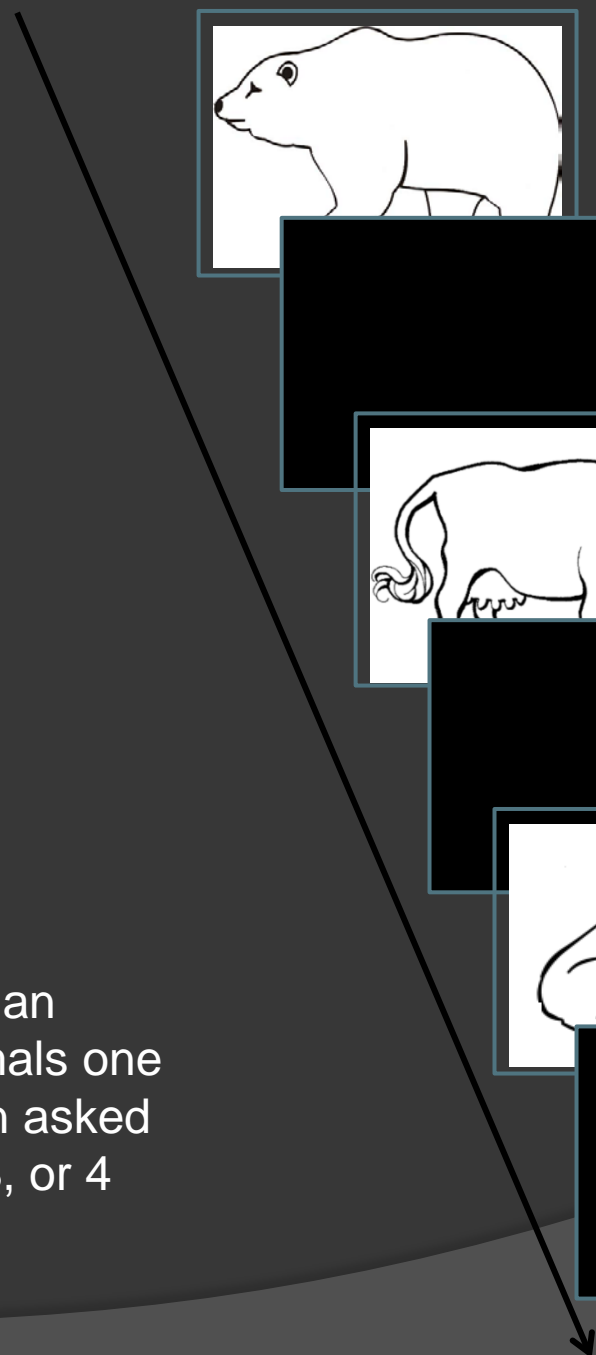
- Growing number patterns
- Function machines
- Arithmetic and algebraic word problems

# Updating/Working Memory tasks

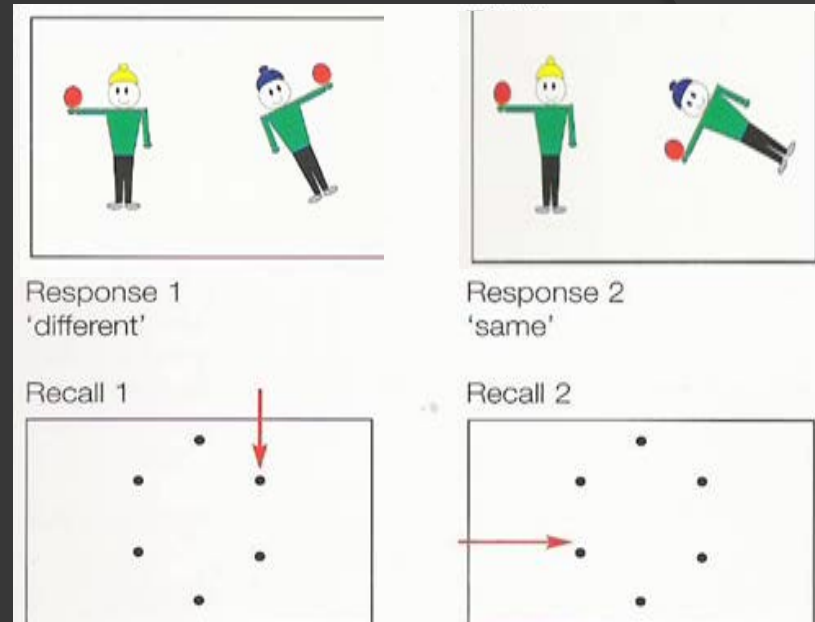


Which were the last two animals that you saw?

Participants were shown an unknown number of animals one at a time. They were then asked to remember the last 2, 3, or 4 animals



◎ Mr. X (AMWA)



◎ Listening Span (AMWA)

- Stimulus
  - Bananas live in water (T/F)
  - Flowers smell *nice* (T/F)
- Response
  - Remember last words in each statement



WIAT

Numerical Operations

## Grade level

## Typical items from the WIAT – Numerical Operations

Kindergarten to  
Primary 1

1 2 3 \_ 5 6 7 8 9

Lower Primary  
(P1 to P3)

$4 + 5 = \underline{\quad}$

$$\begin{array}{r} 150 \\ - 25 \\ \hline \end{array}$$

$4 \times 3 = \underline{\quad}$

Upper Primary  
(P4 to P6)

$$\begin{array}{r} \phantom{0} \\ 7 \overline{)861} \end{array}$$

$.4 + .6 = \underline{\quad}$

$\frac{1}{3} - \frac{1}{4} = \underline{\quad}$

Secondary  
(S1 and above)

$10^2 = \underline{\quad}$

$-14 + (-16) = \underline{\quad}$

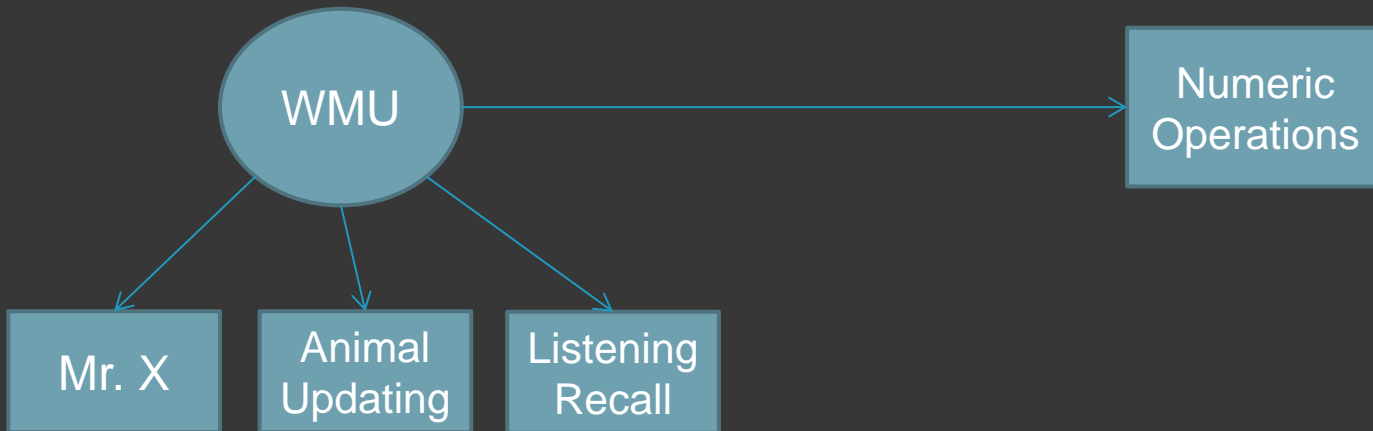
$200\% \text{ of } 80 = \underline{\quad}$

$2x - 15 = 3 - x$

$x = \underline{\quad}$

# Results

# Concurrent Relations

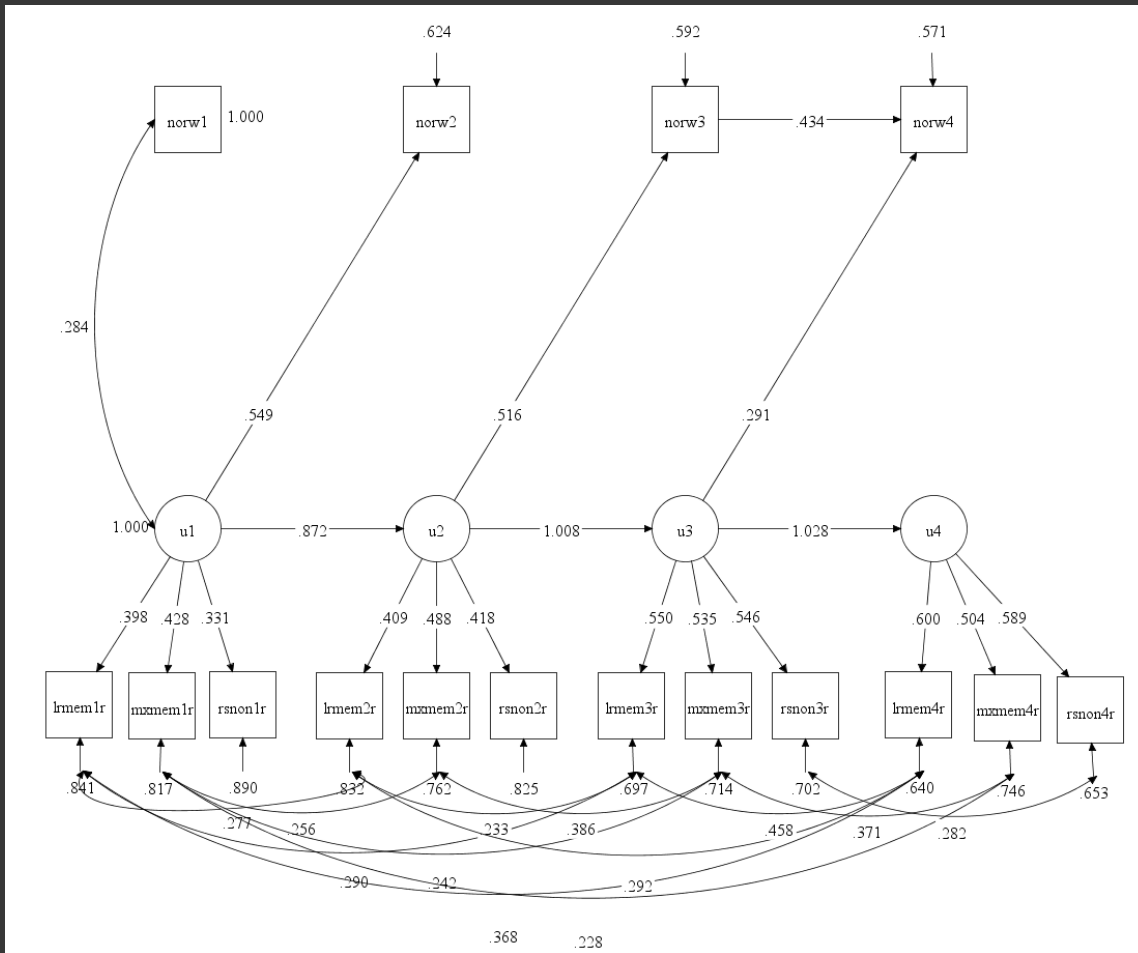


# Concurrent Relations

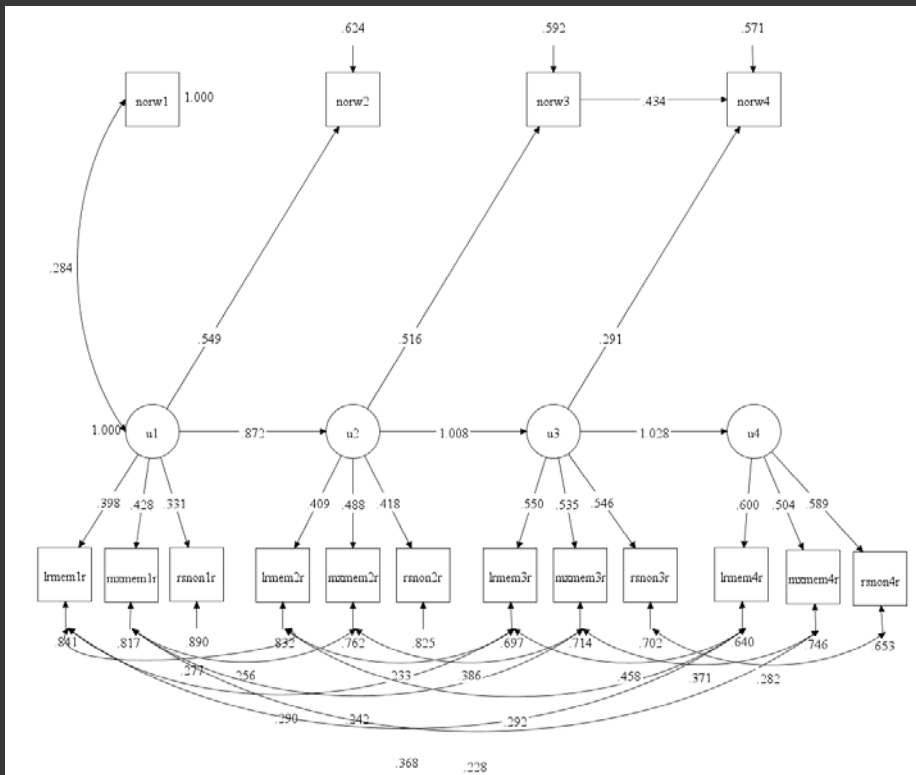
- ◉ With the exception of the youngest children, the cross-sectional findings indicate a strong relation between WMU and mathematical performance
- ◉ Cross-sectional relations between WMU and mathematics peaked at Grades 1 and 2
  - These findings suggest that, at this age, single to multi-digit addition and subtraction rely heavily on WMU capacity
- ◉ Surprising that relation at K1 was relatively small
  - Support the view earlier math skills are more dependent on other fundamental numeric abilities
  - Later math skills, acquired via schooling, being more dependent on general cognitive abilities

| Age           | K2   | P1   | P2   | P3   | P4   | P5   | P6   | S1   | S2   | S3   |
|---------------|------|------|------|------|------|------|------|------|------|------|
| Num Op on WMU | 0.16 | 0.66 | 0.63 | 0.50 | 0.47 | 0.55 | 0.50 | 0.49 | 0.59 | 0.55 |

# Predictive Relations – K2

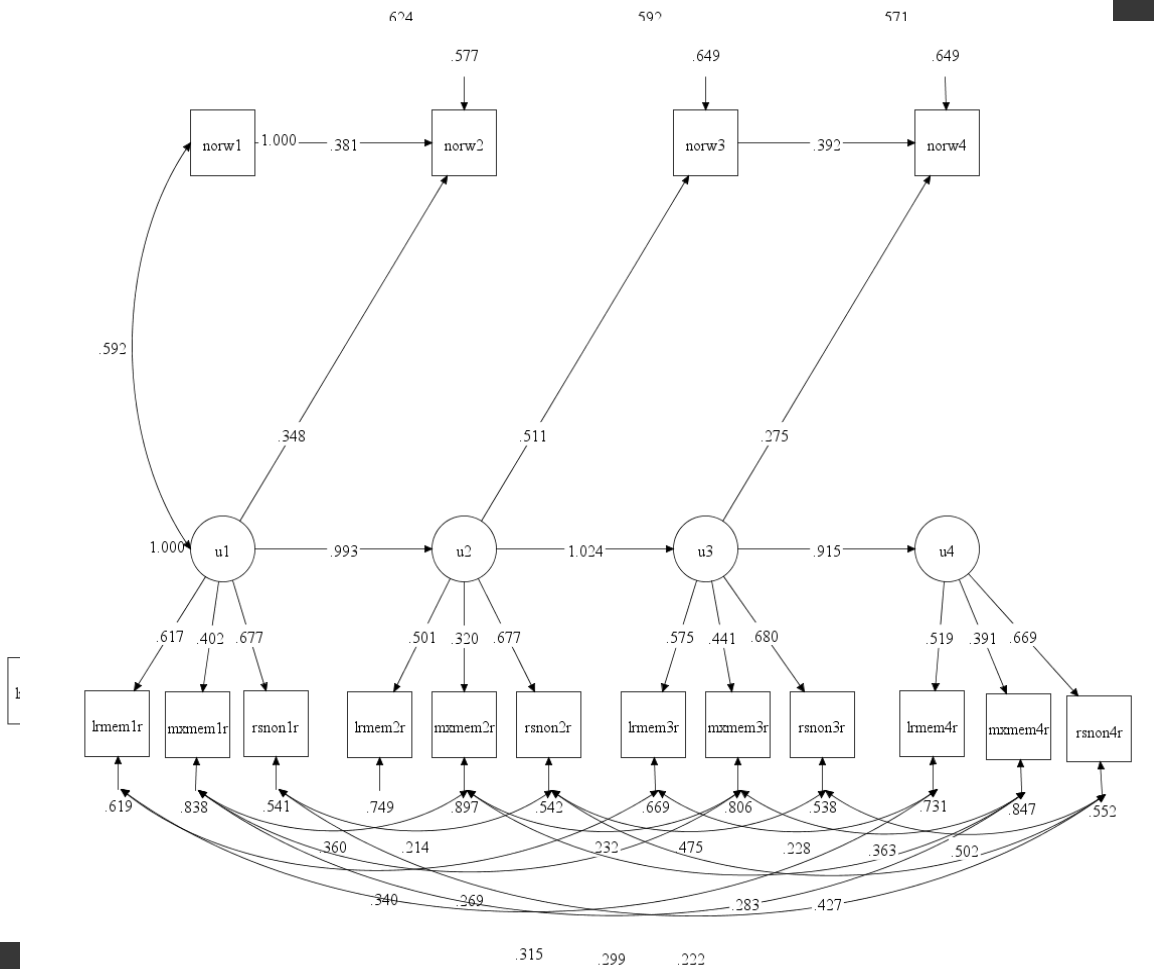


# Predictive Relations



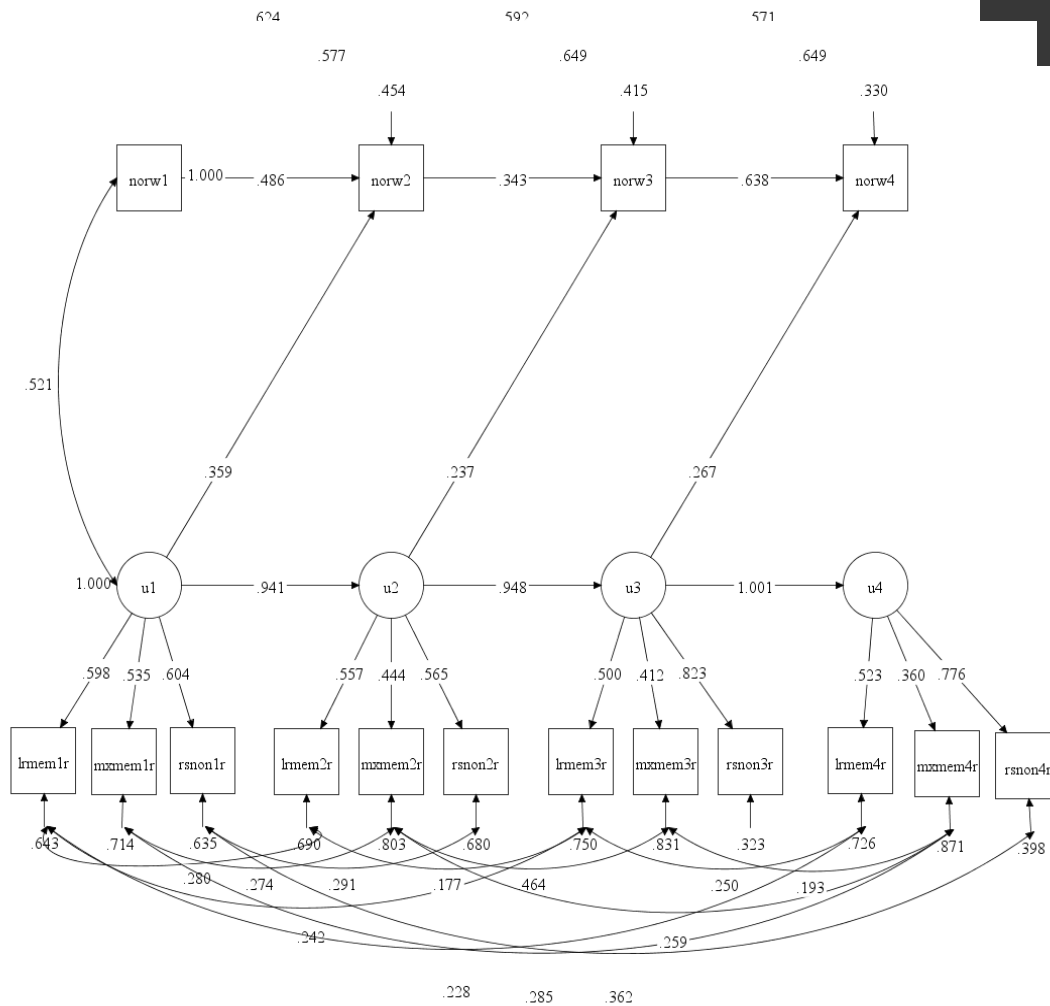
- The predictive findings show that doing well in these early years depends less on what one has learned in mathematics in the previous year, but more on WMU capacity
  - Perhaps indicate that once basic numeracy is mastered, it contributes little to performance in arithmetic computation

# Predictive Relations – P2

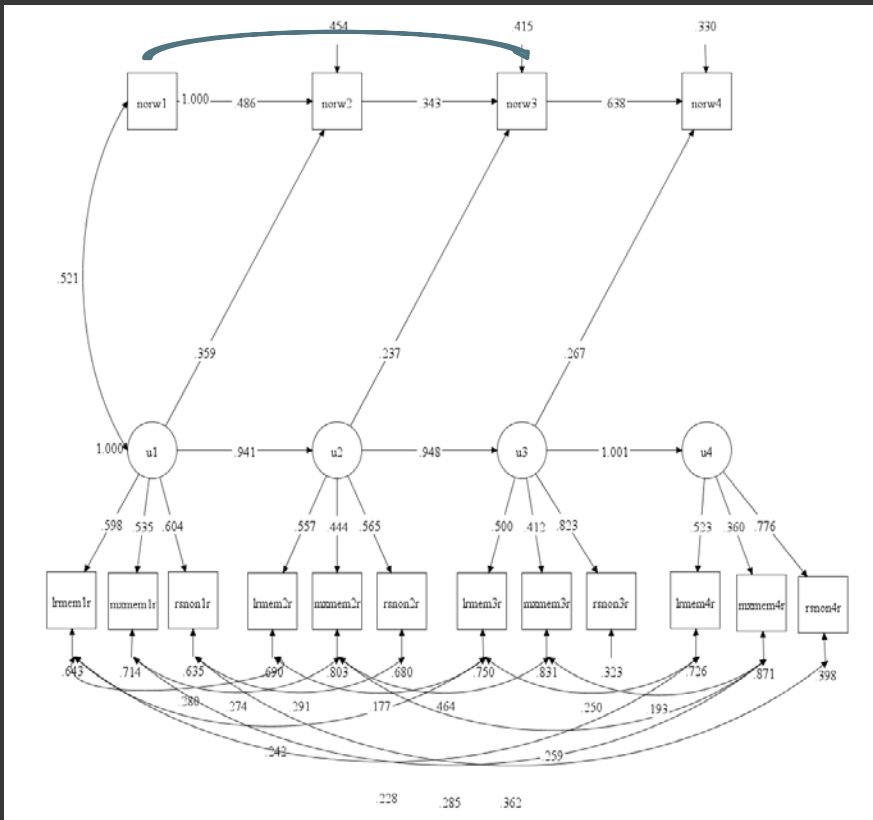




# Predictive Relations – P4

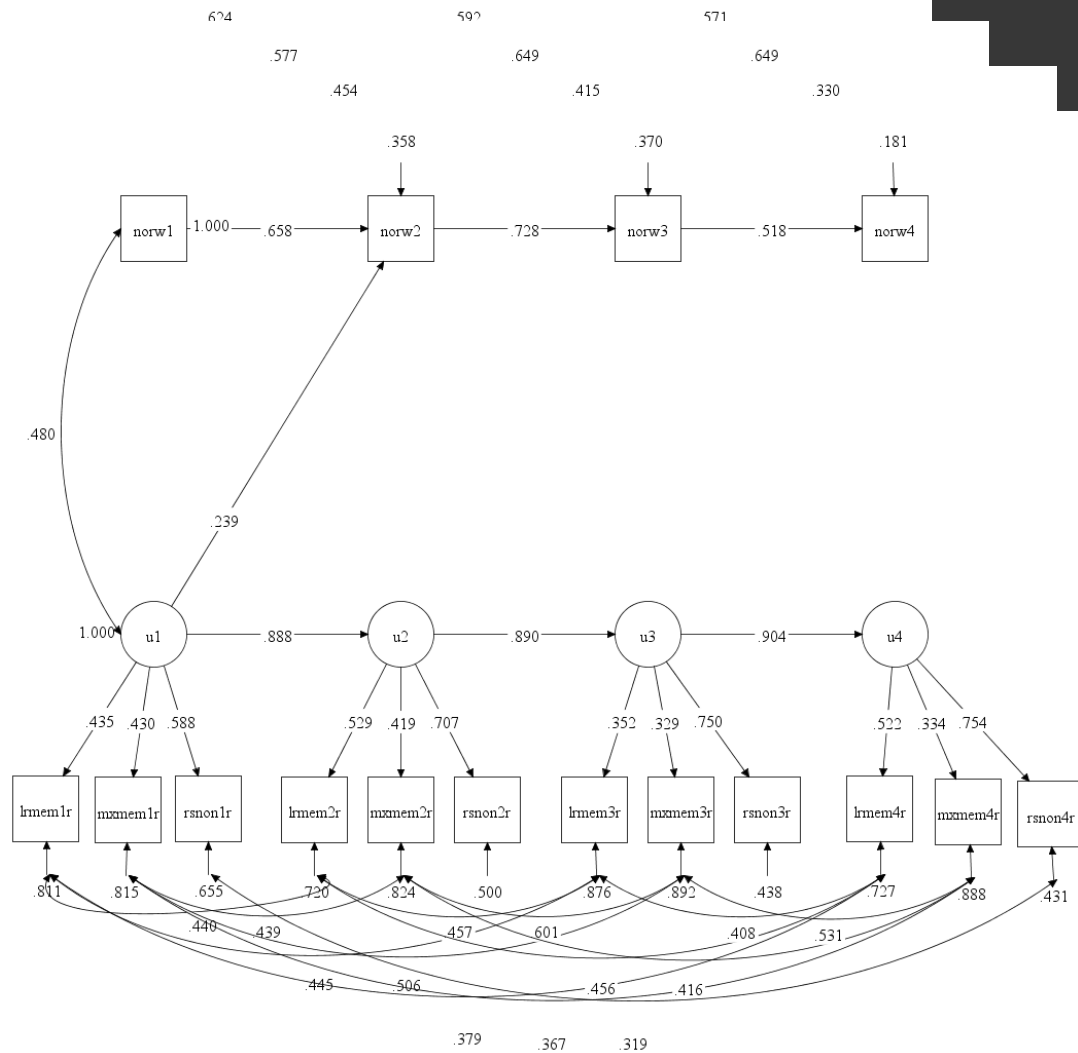


# Predictive Relations – P4

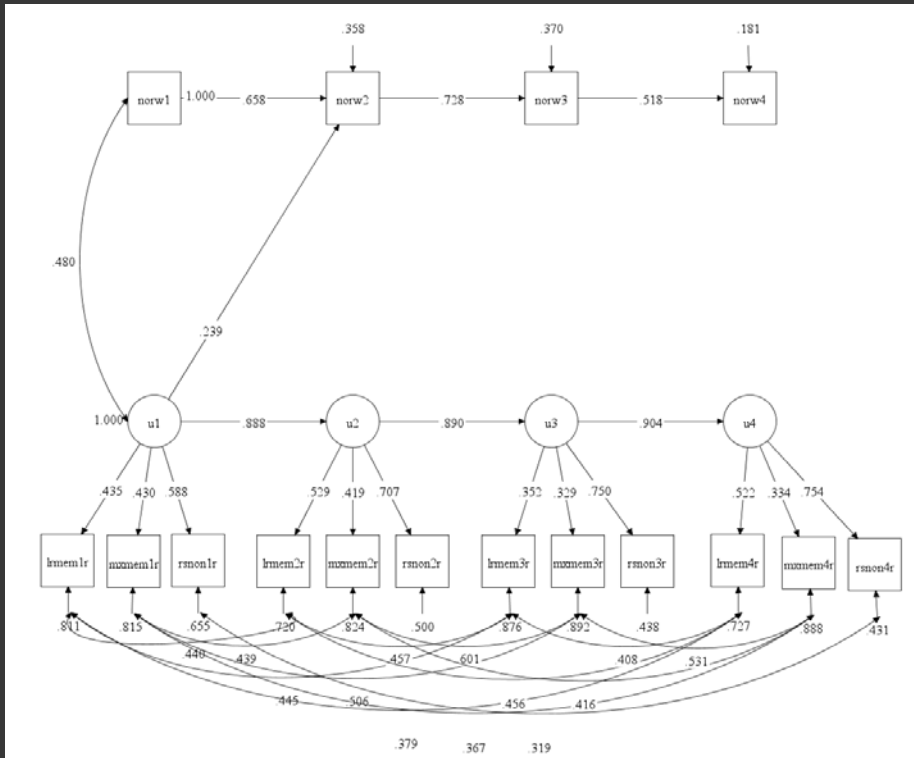


- Math performance at P4 predictive of performances at both P5 and P6
  - simple fraction subtraction and simple addition involving decimals  $\rightarrow$  multi-digit multiplication involving decimals, working with negative integers, and percentages

# Predictive Relations – P6



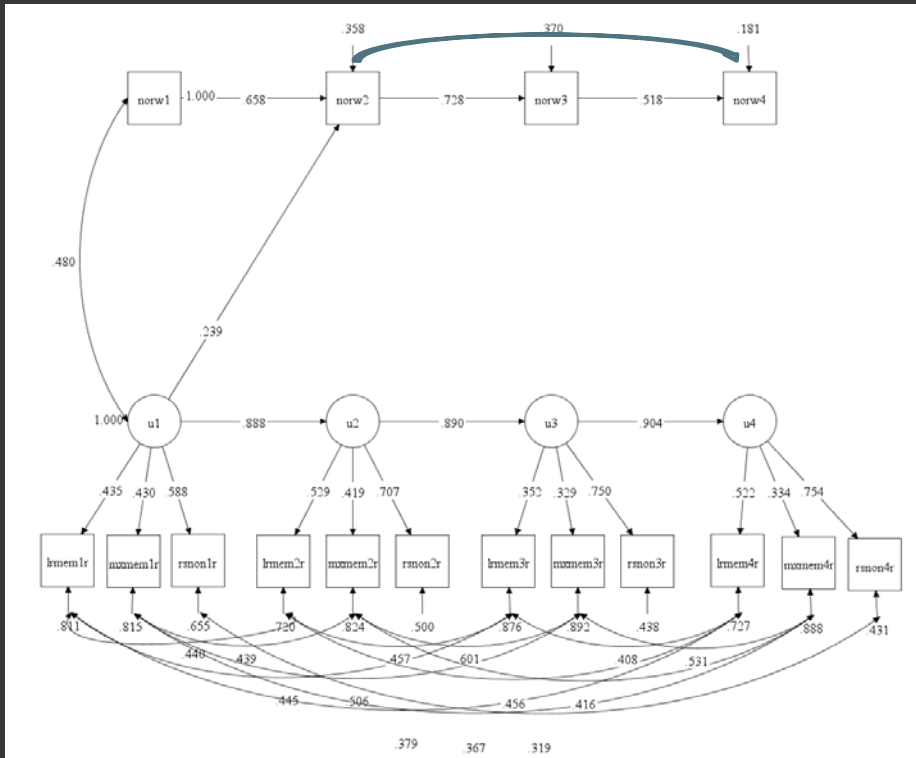
# Predictive Relations – P6



- WMU did not predict subsequent performance in mathematics from S2 to S3

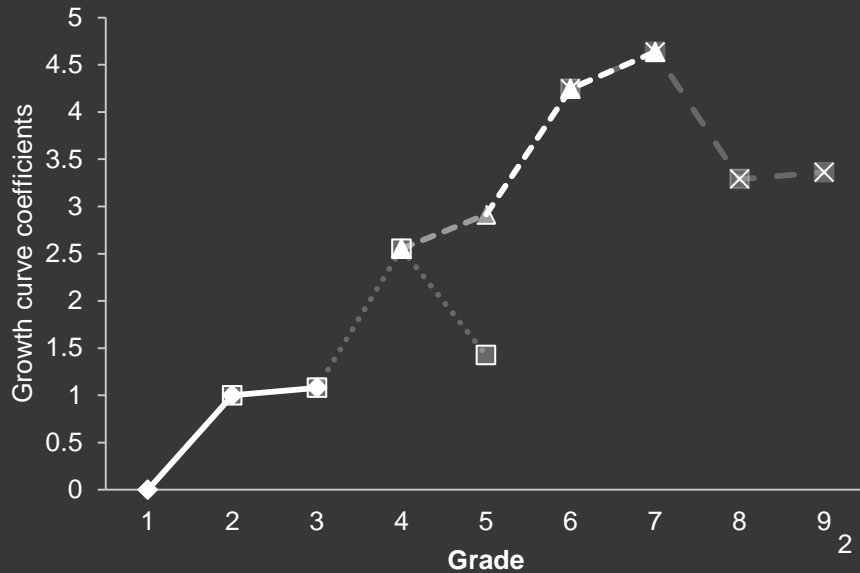
- With increasing expertise, there is a reduction in reliance on effortful executive processes
- The increase in complexity places more demands on domain specific knowledge than on WMU capacities

# Predictive Relations – P6



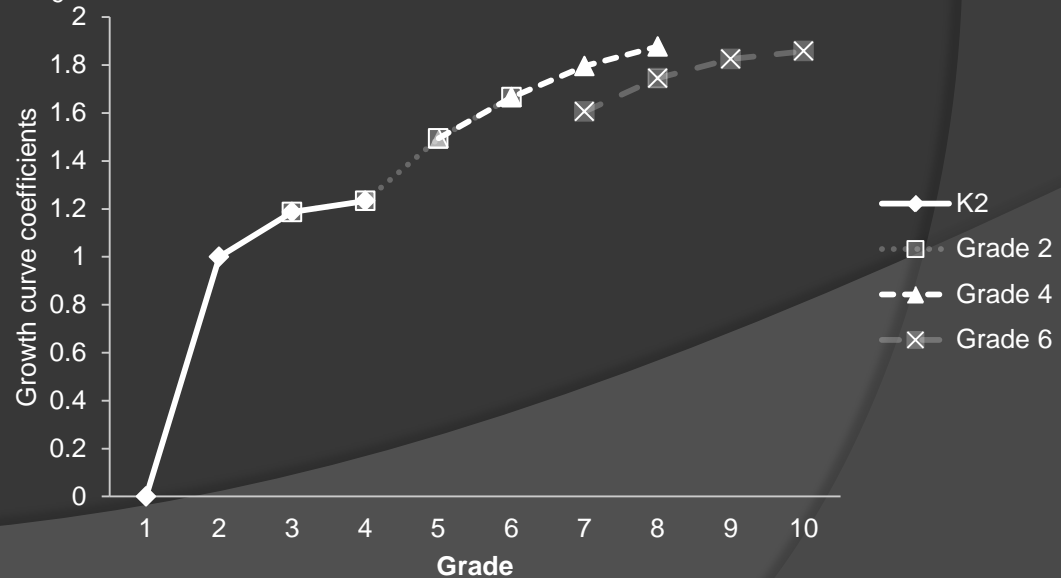
- Math performance at S1 predictive of performances at both S2 and S3
  - simple algebra → questions involving division of fractions and complex exponentials

# Patterns of Growth



Estimated slope coefficients for performance on the Numerical Operations task

Estimated slope coefficients for performance on the WMU



# Patterns of Growth

## ⦿ Mathematics

- Children who had higher scores at kindergarten had lower averaged rates of growth
  - Suggesting that children with lower initial performance do tend to catch up, although not necessarily achieving parity

## ⦿ Updating

- Rates of growth did not differ significantly across individuals

## ⦿ Updating and mathematics

- Children who entered kindergarten with higher updating capacity improved in their mathematics performance faster than did children with lower updating capacity

# Conclusions

## ◎ Several important findings

- Relation between Updating and Math peaked at P1 and P2
- Children with higher updating capacity improved in their mathematics performance faster
- Predictive relations between Updating and Math were significant from K2 to S1
- Performance in math at P1 and P2 not reliant on earlier math performance

## ◎ Implications

- For secondary school students, math content knowledge is more important than underlying cognitive capacity
  - Focus of teaching should be placed on domain specific content
- For the first years of primary schooling, updating capacity is important
  - Can updating capacity be improved? How?
    - Stay tuned ...

Caveat: not all early numeracy capacities were measured – Rebecca's talk



# Applied Cognitive Development Lab

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- Research Scientists/Fellows
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  - Fannie Khng
  - Ng EeLynn
- Research Assistants
  - Jeremy Ng
  - Jennifer Ang
  - Juliana Koh
  - Lim Aik Meng
  - Tay Jia Xin
- Project manager
  - Yvonne Ng



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